## Pre-Exam - Unit 5 - Momentum - Free Responsive Questions

1. C2004M1.


A rope of length $L$ is attached to a support at point $C$. A person of mass $m_{1}$ sits on a ledge at position $A$ holding the other end of the rope so that it is horizontal and taut, as shown. The person then drops off the ledge and swings down on the rope toward position $B$ on a lower ledge where an object of mass $m_{2}$ is at rest. At position $B$ the person grabs hold of the object and simultaneously lets go of the rope. The person and object then land together in the lake at point $D$, which is a vertical distance $L$ below position $B$. Air resistance and the mass of the rope are negligible. Derive expressions for each of the following in terms of $m_{1}, m_{2}, L$, and $g$.
a. The speed of the person just before the collision with the object
b. The tension in the rope just before the collision with the object
c. The speed of the person and object just after the collision
d. The total horizontal displacement $x$ of the person from position $A$ until the person and object land in the water at point $D$.
2.


2001M1. A motion sensor and a force sensor record the motion of a cart along a track, as shown above. The cart is given a push so that it moves toward the force sensor and then collides with it. The two sensors record the values shown in the following graphs.
a. Determine the cart's average acceleration between $t=0.33 \mathrm{~s}$ and $\mathrm{t}=0.37 \mathrm{~s}$.
b. Determine the magnitude of the change in the cart's momentum during the collision.
c. Determine the mass of the cart.
d. Determine the energy lost in the collision between the force sensor and the cart
3. 2008B1


Several students are riding in bumper cars at an amusement park. The combined mass of car $A$ and its occupants is 250 kg . The combined mass of car $B$ and its occupants is 200 kg . Car $A$ is 15 m away from car $B$ and moving to the right at $2.0 \mathrm{~m} / \mathrm{s}$, as shown, when the driver decides to bump into car $B$, which is at rest.
a. Car $A$ accelerates at $1.5 \mathrm{~m} / \mathrm{s}^{2}$ to a speed of $5.0 \mathrm{~m} / \mathrm{s}$ and then continues at constant velocity until it strikes car. Calculate the total time for car $A$ to travel the 15 m .
b. After the collision, car $B$ moves to the right at a speed of $4.8 \mathrm{~m} / \mathrm{s}$.
i. Calculate the speed of car $A$ after the collision.
ii. Indicate the direction of motion of car $A$ after the collision.
$\qquad$ To the left $\qquad$ To the right $\qquad$ None; car $A$ is at rest.
c. Is this an elastic collision?
$\qquad$ Yes $\qquad$ No
Justify your answer. (hint will take math!!!)
4.


2002B1B. A 2.0 kg frictionless cart is moving at a constant speed of $3.0 \mathrm{~m} / \mathrm{s}$ to the right on a horizontal surface, as shown above, when it collides with a second cart of undetermined mass $m$ that is initially at rest. The force $F$ of the collision as a function of time $t$ is shown in the graph below, where $t=0$ is the instant of initial contact. As a result of the collision, the second cart acquires a speed of $1.6 \mathrm{~m} / \mathrm{s}$ to the right. Assume that friction is negligible before, during, and after the collision.

Force $F(\mathrm{kN})$

(a) Calculate the magnitude and direction of the velocity of the 2.0 kg cart after the collision.
(b) Calculate the mass $m$ of the second cart.

After the collision, the second cart eventually experiences a ramp, which it traverses with no frictional losses. The graph below shows the speed $v$ of the second cart as a function of time $t$ for the next 5.0 s , where $t=0$ is now the instant at which the carts separate.

(c) Calculate the acceleration of the cart at $t=3.0 \mathrm{~s}$.
(d) Calculate the distance traveled by the second cart during the 5.0 s interval after the collision ( $0 \mathrm{~s}<t<5.0 \mathrm{~s}$ ).
(e) State whether the ramp goes up or down and calculate the maximum elevation (above or below the initial height) reached by the second cart on the ramp during the 5.0 s interval after the collision ( $0 \mathrm{~s}<t<5.0 \mathrm{~s}$ ).


Note: Figures not drawn to scale.
2001B2. An incident ball A of mass 0.10 kg is sliding at $1.4 \mathrm{~m} / \mathrm{s}$ on the horizontal tabletop of negligible friction as shown above. It makes a head-on collision with a target ball B of mass 0.50 kg at rest at the edge of the table. As a result of the collision, the incident ball rebounds, sliding backwards at $0.70 \mathrm{~m} / \mathrm{s}$ immediately after the collision.
A. Calculate the speed of the 0.50 kg target ball immediately after the collision.

The tabletop is 1.20 m above a level, horizontal floor. The target ball is projected horizontally and initially strikes the floor at a horizontal displacement $d$ from the point of collision.

## B. Calculate the horizontal displacement

In another experiment on the same table, the target ball $B$ is replaced by target ball $C$ of mass 0.10 kg . The incident ball A again slides at $1.4 \mathrm{~m} / \mathrm{s}$, as shown below left, but this time makes a glancing collision with the target ball C that is at rest at the edge of the table. The target ball C strikes the floor at point P , which is at a horizontal displacement of 0.15 m from the point of the collision, and at a horizontal angle of $30^{\circ}$ from the +x -axis, as shown below right.


Top View
Before Collision


Top View
After Collision
C. Calculate the speed $v$ of the target ball $C$ immediately after the collision.
D. Calculate the y-component of incident ball A's momentum immediately after the collision.

