## NEWTON'S $3{ }^{\text {RD }}$ LAW



- For every action there is an equal and opposite reaction
- The astronaut pushes on the rock and the rock pushes on the astronaut
"If object 1 and object 2 interact, the force $F_{12}$ exerted by object 1 on object 2 is equal in magnitude but opposite in direction to the force $F_{21}$ exerted by object 2 on object 1."

$$
F_{12}=-F_{21}
$$

Forces in nature always exist in pairs, as an interaction between two objects.
We represent this in a system schema with arrows that point both directions.

## NEWTON'S THIRD LAW (ACTION AND REACTION)

Every force is part of an interaction between two objects.
This interaction makes up an action-reaction pair.
If you can switch the order of objects, you have an action-reaction pair.
Use the phrase: Force with which A pulls (or pushes) B
The reaction is: Force with which B pulls(or pushes) A Equal and Opposite
Fn and FG are NOT !

Warning: When drawing an FBD for an object, you will never have an action-reaction pair. Only one of these forces can act on the object.

## FRICTION

Friction - is the force that resists the sliding of one object past another.

- In free-body diagrams, the force of friction is always parallel to the surface of contact.
- Force of friction $\left(F_{f}\right)$ is proportional to the magnitude of the normal force $\left(F_{N}\right)$
- Depends upon
- Kinds of materials
- How much they are pressed together


## 2 TYPES OF FRICTION

## Kinetic Friction:

- Kinetic Friction describes the contact force resisting the relative motion between two objects when one or both are moving
- The direction of the force of friction is always parallel to the plane of contact between the objects (perpendicular to the normal force) and opposite of the direction of motion


## Static Friction:

- Staic Friction describes the contact force resisting the relative motion between two objects when neither object is moving (relative to the other)
- The force of static friction can vary depending on the force it's opposing, up to a maximum amount


## STATIC FRICTION

The static force of friction opposes the relative motion that would occur if there were no friction.

Another interesting feature is that the static force of friction adjusts itself to whatever it needs to be to prevent relative motion between the surfaces in contact.

Within limits, that is. The static force of friction has a maximum value, Ffsmax

## FORCE OF FRICTION

## Calculating Frictional Force:

Both static and kinetic friction depend on two factors:

- The normal force (which measures how strongly the two objects are pushed together)
- The coefficient of friction (which measures the microscopic "roughness" of the surfaces that are in contact with each other)
- The coefficient of friction is a property of the two materials that are in contact with each other and has a different value for static and kinetic friction. It's represented by the Greek letter $\mu$.

Coefficient of static friction: $\mu_{s} \quad$ Coefficient of kinetic friction: $\mu_{k}$

## 2 TYPES OF FRICTION

1. Object is not moving

- Static friction $\left(F_{s f}\right)$ is a force that resists the start of sliding motion between two surfaces that are in contact and at rest
- As long as object doesn't move $F_{s}=-F_{\text {applied }}$
- Maximum force of $F_{s}$ is $F_{s, \max }$
- $F_{s, M a x}$ - Just before movement starts
- $F_{s, \max }=\mu_{\mathrm{s}} \mathrm{F}_{\mathrm{N}}$
- $\mu_{\mathrm{s}}=$ coefficient of static friction
- $\mu_{\mathrm{s}}$ depends upon the two surfaces


## 2 TYPES OF FRICTION (CONT)

2. Object is moving

- Kinetic friction $\left(F_{k}\right)$ is the force that opposes the movement of two surfaces that are in contact and are sliding over each other.
- Kinetic friction is always less than the maximum static friction.
- $F_{k}=\mu_{k} F_{N}$
- $\mu_{\mathrm{k}}=$ coefficient of kinetic friction
- For any pair of surfaces $\mu_{\mathrm{k}}<\mu_{\mathrm{s}}$
- It's harder to push an object from rest than it is to keep it in motion


## COEFFICIENTS OF FRICTIONTABLE



## SAMPLE PROBLEM-FRICTION



A Student attaches a rope to a 20.0 kg box of books. He pulls with a force of 90.0 N at an angle of $30.0^{\circ}$ with the horizontal. The coefficient of kinetic friction between the box and the sidewalk is 0.500 . Find the acceleration of the box.

Given:

$$
\begin{aligned}
& m=20.0 \mathrm{~kg} \\
& \mu_{k}=0.500 \\
& \mathrm{~F}_{\text {applied }}=90.0 \mathrm{~N} \\
& \text { Angle }=30.0^{\circ}
\end{aligned}
$$

Unknown:

$$
\mathbf{a}=\text { ? }
$$



## SAMPLE PROBLEMFRICTION

- Any vectors not on X \& Y axis break it


$$
\begin{aligned}
& \text { into its components } \\
& \begin{aligned}
F_{a x} & =F_{a} \operatorname{Cos} \theta \\
F_{a x} & =(90.0 \mathrm{~N}) \operatorname{Cos} 30.0^{\circ} \\
& =77.9 \mathrm{~N}
\end{aligned}
\end{aligned}
$$

$$
F_{a y}=F a \operatorname{Sin} \theta
$$

$$
\begin{aligned}
\mathrm{F}_{\mathrm{ay}} & =(90.0 \mathrm{~N}) \operatorname{Sin} 30.0^{\circ} \\
& =45.0 \mathrm{~N}
\end{aligned}
$$

Sum of Forces in Y-Direction

$$
\Sigma F_{y}=\text { ma }_{y} \text { no motion in } y
$$

Sum of Forces in X-Direction

$$
F_{a y}-F_{w}+F_{n}=0
$$

$$
\begin{aligned}
& \Sigma F_{x}=m a_{x} \\
& F_{a x}-F_{k}=m a \\
& \quad F_{k}=U_{k} F_{n} \quad \text { Sub into eqn } \\
& F_{a x}-U_{k} F_{n}=m a
\end{aligned}
$$

$$
F_{n}=F_{w}-F_{a y} \quad F_{w}=M g
$$

$$
F_{n}=M g-F_{a y}
$$

$$
F_{n}=(20.0 \mathrm{~kg})\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right)-45.0 \mathrm{~N}
$$

$$
F_{n}=151
$$

## SAMPLE PROBLEM-FRICTION

$$
\mathrm{F}_{\mathrm{ax}}-\mathrm{U}_{\mathrm{k}} \mathrm{~F}_{\mathrm{n}}=\mathrm{ma} \mathrm{x}_{\mathrm{x}}
$$

$$
a_{x}=\frac{F_{\text {applied }, x}-F_{k}}{m}=\frac{77.9 \mathrm{~N}-75.5 \mathrm{~N}}{20.0 \mathrm{~kg}}=\frac{2.4 \mathrm{~N}}{20.0 \mathrm{~kg}}=\frac{2.4 \mathrm{~kg} \bullet \mathrm{~m} / \mathrm{s}^{2}}{20.0 \mathrm{~kg}}
$$

$\mathrm{a}=0.12 \mathrm{~m} / \mathrm{s}^{2}$ to the right

