

[Energy]

- **Identify** several forms of energy
- **Calculate** kinetic energy for an object
- **Apply** the work-kinetic energy theorem to solve problems
- **Distinguish** between kinetic & potential energy
- **Classify** different types of potential energy
- **Calculate** the potential energy associated with an object's position

[Energy]

- **Energy** is “something” that enables an object to do work
- What is that something?
 - Energy is associated with heat, light, electricity, mechanical motion, sound, and the nature of a chemical reaction
- Objects/systems can have energy and can **transfer** energy or **transform** it
- Energy can be transferred between objects/systems, which we call “doing work.” Work done on a system is equal to the amount of energy given or taken away from a system.
 $W = \Delta E$

[Types of Energy]

- $K = \frac{1}{2}mv^2$ Kinetic Energy
- $U_s = \frac{1}{2}kx^2$ Potential Spring Energy
- $U_g = mg\Delta y$ or mgh Potential Gravity Energy
- $\Delta E_{\text{thermal}} = F_k d$ Thermal energy
 - heat energy from friction/air resistance
- $E_{\text{mechanical}} = K + U_g + U_s$ (doesn't not include thermal energy)
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[Important points]

- Kinematic eqns can ONLY be used when $a = \text{constant}$ (free fall)
- Energy equations can be used when $a \neq \text{constant}$ (roller coaster)
- Sound, heat, deformation, etc are common examples of energy loss

Kinetic Energy

- **Kinetic Energy** depends on speed and mass
 - Units – Joules (used for all forms of energy)
 - $\text{kg}\cdot\text{m}^2/\text{s}^2$ or $\text{N}\cdot\text{m}$ or J

kinetic energy

$$K = \frac{1}{2}mv^2$$

K = kinetic energy
m = mass
v = velocity

Kinetic Example Problem

- A 100. Kg Linebacker moves at 8.90 m/s (runs 100m in 11.2 secs). How much KE does the linebacker have? How fast does a 54.5 Kg wide receiver have to run to have the same KE as the linebacker?

Given: Linebacker Wide Receiver

$$V_L = 8.90 \text{ m/s} \quad V_w = ?$$

$$M_L = 100. \text{ kg} \quad M_w = 54.5 \text{ kg}$$

$$KE_L = ?$$

$$KE_w = KE_L$$

$$\frac{1}{2} M_w V_w^2 = KE_L$$

$$V_w^2 = 2KE_L / M_w$$

$$V_w^2 = 2 (3.96 \times 10^3 \text{ J}) / (54.5 \text{ kg})$$

$$V_w = 12.1 \text{ m/s}$$

Soln:

$$KE_L = \frac{1}{2} M_L V_L^2$$

$$= \frac{1}{2} (100. \text{ Kg}) (8.90 \text{ m/s})^2$$

$$KE_L = 3.96 \times 10^3 \text{ J}$$

note: wide receiver would have to run 100m in 8.26 secs

Work-Kinetic Energy Theorem

- Another way of defining work is in terms of what it does: work done on an object changes the energy of that object. This is called the **Work-Energy Theorem**
- The net work (W_{net}) done on an object is equal to the change in the KE of the object

WORK-KINETIC ENERGY THEOREM

$$W_{net} = \Delta KE$$

net work = change in kinetic energy

$$W_{net} = \Delta KE = \frac{1}{2} mv_f^2 - \frac{1}{2} mv_i^2$$

When Velocity is constant $\Delta KE = 0$ then work is zero

Potential Energy

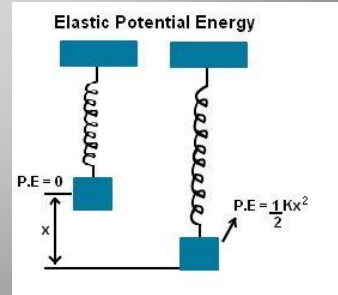
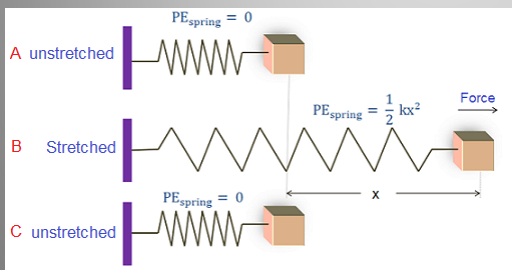
- Potential Energy** is the energy associated with an object because of the position, shape, or condition of the object.
 - Stored energy
 - Chemical energy
 - Object due to its position (Gravitational, ex: rock on hilltop)
 - Elastic potential energy
- Gravitational potential energy** is the potential energy stored in the gravitational fields of interacting bodies.
 - depends on height from a zero level (zero level is arbitrary)

$$U_g = mgh$$

$$U_{\text{gravitational}} = \text{mass} \times \text{free-fall acceleration} \times \text{height}$$

Potential Energy

- Elastic Potential energy
 - The energy available for use in deformed elastic objects
 - Rubber bands, springs in trampolines, pole-vault poles, muscles
 - For springs, the distance compressed or stretched = Δx



Sample Problem: Elastic potential energy

A 70.0 kg stuntman is attached to a bungee cord with an unstretched length of 15.0 m. He jumps off a bridge spanning a river from a height of 50.0 m. When he finally stops, the cord has stretched a length of 44.0 m. Disregard the weight of the bungee cord. Assuming the spring constant of the bungee cord is 71.8 N/m, what is the total potential energy relative to the water when the man stops falling?

Given:

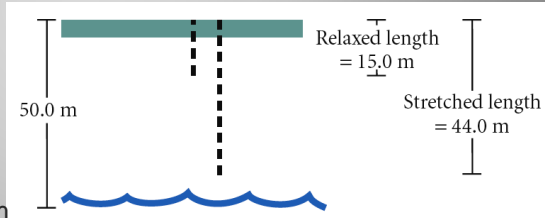
$$m = 70.0 \text{ kg}$$

$$k = 71.8 \text{ N/m}$$

$$g = 9.8 \text{ m/s}^2$$

$$h = 50.0 \text{ m} - 44.0 \text{ m} = 6.0 \text{ m}$$

$$x = 44.0 \text{ m} - 15.0 \text{ m} = 29.0 \text{ m}$$



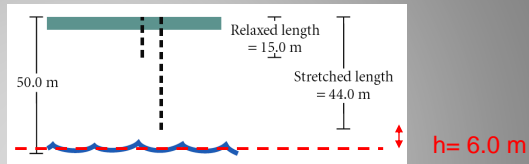
$$U_g = 0 \text{ J at river level}$$

$$U_{\text{tot}} = ?$$

Sample Problem: Elastic potential energy

The zero level for U_g is chosen to be at the surface of the water.

$$h = 50.0 \text{ m} - 44.0 \text{ m} = 6.0 \text{ m}$$



The total Potential Energy is the sum of PE_g and PE_{elastic}

$$U_{\text{tot}} = 4.1 \times 10^3 \text{ J} + 3.02 \times 10^4 \text{ J}$$

$$U_{\text{tot}} = U_g + U_{\text{elastic}}$$

$$U_g = mgh$$

$$= (70.0 \text{ kg})(9.81 \text{ m/s}^2)(6.0 \text{ m}) = 4.1 \times 10^3 \text{ J}$$

$$U_{\text{elastic}} = \frac{1}{2} kx^2$$

$$= \frac{1}{2} (71.8 \text{ N/m})(29.0 \text{ m})^2 = 3.02 \times 10^4 \text{ J}$$

$$U_{\text{tot}} = 3.43 \times 10^4 \text{ J}$$